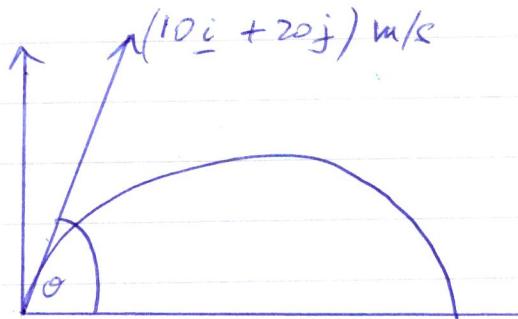


(10)  $\rightarrow$

S	U	V	A	T
X	10	$V_x$	0	3

S	U	V	A	T
Y	20	$V_y$	-9.8	2



So  $\rightarrow$  :  $S = ut + \frac{1}{2}at^2 \Rightarrow X = 10(3) + 0 = 30$

$\uparrow$  :  $S = ut + \frac{1}{2}at^2 \Rightarrow Y = 20(3) - \frac{1}{2}(10)(9) = 15$

So  $\underline{S} = (30\hat{i} + 15\hat{j}) \text{ m}$

For Velocity vector  $v = u + at$ . So

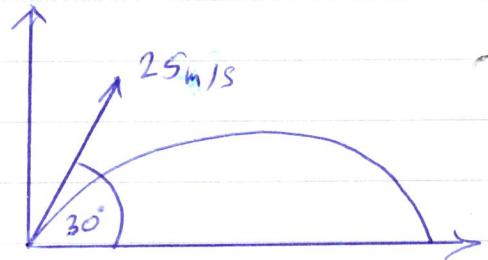
$$(\rightarrow) : V_x = 10 + 0(3) = 10$$

$$(\uparrow) : V_y = 20 - 10(3) = -10$$

$$\text{So } \underline{v} = (10\hat{i} - 10\hat{j}) \text{ m/s}$$

$$\textcircled{11} \begin{array}{l} (\rightarrow) \\ x \end{array} \begin{array}{l} S \\ U \\ V \\ A \\ T \end{array} \begin{array}{l} 25 \cos 30 \\ 25 \cos 30 \\ V_x \\ 0 \\ 2\frac{1}{2} \end{array}$$

$$\begin{array}{l} (\uparrow) \\ y \end{array} \begin{array}{l} S \\ U \\ V \\ A \\ T \end{array} \begin{array}{l} 25 \sin 30 \\ 25 \sin 30 \\ V_y \\ -9.8 \\ 2\frac{1}{2} \end{array}$$



$$(\rightarrow) : v = u + at \Rightarrow V_x = 25 \cos 30 + 0 = 21.65$$

$$(\uparrow) : v = u + at \Rightarrow V_y = 25 \sin 30 - (9.8)(2\frac{1}{2}) = -12$$

So horizontal velocity is 21.65 m/s

& vertical velocity is 12 m/s downward

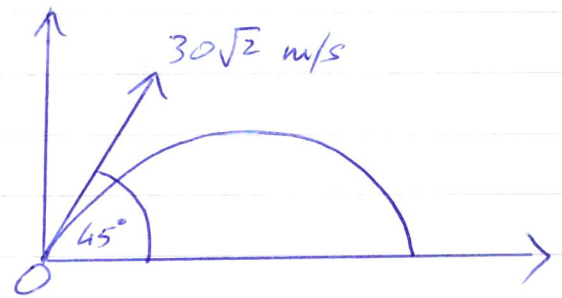
$$\text{Speed after } t = 2\frac{1}{2} \text{ sec} : v = \sqrt{(21.65)^2 + (12)^2} \\ = 24.75 \text{ m/s}$$

$$\text{Direction: } \theta = \tan^{-1} \frac{-12}{21.65} = -29^\circ$$

or  $29^\circ$  below horizontal.

(12)

	S	U	V	A	T
(→)	x	$30\sqrt{2}\cos 45$	$v_x$	0	2
(↑)	y	$30\sqrt{2}\sin 45$	$v_y$	-9.8	2



$$\text{So : } (\rightarrow) : S = ut + \frac{1}{2}at^2 \Rightarrow x = (30\sqrt{2}\cos 45)(2) + 0 = 60$$

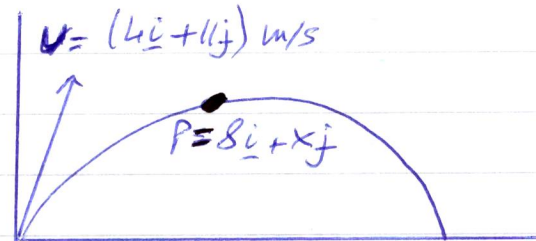
$$(\uparrow) : S = ut + \frac{1}{2}at^2 \Rightarrow y = (30\sqrt{2}\sin 45)(2) - \frac{1}{2}(9.8)(4) = 40.4$$

So horizontal displacement is 60 m & vertical displacement is 40.4 m

$$\therefore \text{Distance From } O = \sqrt{60^2 + 40.4^2} = 72.33 \text{ m}$$

(13)

	S	U	V	A	T
(→)	8	4	$v_x$	0	t
(↑)	x	11	$v_y$	-10	t

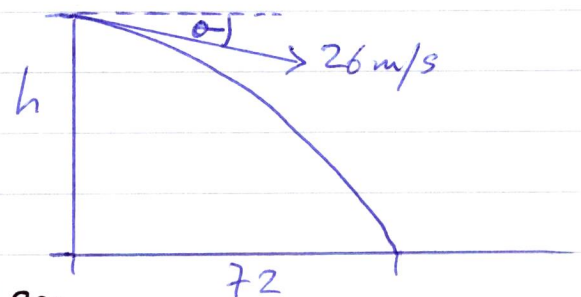


$$\text{So : } (\rightarrow) : S = ut + \frac{1}{2}at^2 \Rightarrow 8 = 4t \Rightarrow t = 2 \text{ sec}$$

$$(\uparrow) : S = ut + \frac{1}{2}at^2 \Rightarrow x = 11(2) - \frac{1}{2}(10)(4) = 2 \text{ m}$$

(14)

	S	U	V	A	T
(→)	72	$26\cos\theta$		0	t
(↑)	h	$26\sin\theta$		-10	t

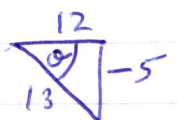


$$\text{So : } (\rightarrow) S = ut + \frac{1}{2}at^2$$

$$\text{i.e. } 72 = [26(\cos\theta)]t + 0 \Rightarrow t = 3 \text{ sec}$$

$$\downarrow \frac{12}{13}$$

$$\tan\theta = \frac{5}{12}$$



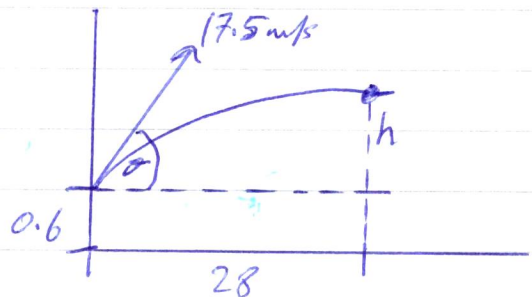
$$(\uparrow): S = ut + \frac{1}{2}at^2 \Rightarrow h = (26 \sin \theta)t - \frac{10}{2}(t^2),$$

with  $t = 3$ . So  $h = 26 \left(\frac{-5}{13}\right)(3) - \frac{10}{2}(9)$   
 $= -75 \text{ m i.e. } 75 \text{ m downward}$

(15)

	S	U	V	A	T
( $\rightarrow$ )	28	$17.5 \cos \theta$		0	t
( $\uparrow$ )	h	$17.5 \sin \theta$		-9.8	t

So ( $\rightarrow$ ):  $S = ut + \frac{1}{2}at^2$   
 $\therefore 28 = \left[17.5 \left(\frac{4}{5}\right)\right]t + 0$   
 $\Rightarrow t = 2 \text{ Sec}$



$\tan \theta = \frac{3}{4}$

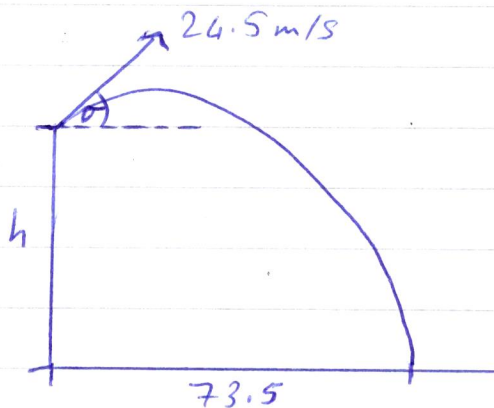
And ( $\uparrow$ ):  $S = ut + \frac{1}{2}at^2 \Rightarrow h = \left[17.5 \left(\frac{3}{5}\right)\right](2) - \frac{1}{2}(9.8)2^2$   
 $= 21 - 19.6 = 1.4 \text{ m}$

Ball is already 0.6 m above ground level so height of ball above ground level is  $1.4 + 0.6 = 2 \text{ m}$ .

(16)

	S	U	V	A	T
( $\rightarrow$ )	73.5	$24.5 \cos \theta$		0	t
( $\uparrow$ )	h	$24.5 \sin \theta$		-9.8	t

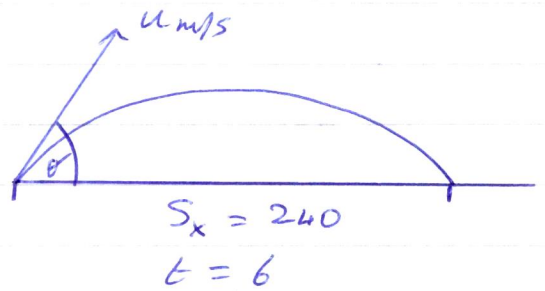
So ( $\rightarrow$ ):  $S = ut + \frac{1}{2}at^2$   
 $\Rightarrow 73.5 = 24.5 \left(\frac{3}{5}\right)t + 0$   
 $\Rightarrow t = 5 \text{ sec}$



$\tan \theta = \frac{4}{3}$

( $\uparrow$ ):  $S = ut + \frac{1}{2}at^2 \Rightarrow h = 24.5 \left(\frac{4}{5}\right)(5) - \frac{9.8}{2}(5)^2 = -24.5 \text{ m}$   
 i.e. ball lands 24.5 m below Throwing point  $\Rightarrow$  tower height is 24.5 m

(17)	S	U	V	A	T
(→)	240	$u \cos \theta$	?	0	6
(↑)	0	$u \sin \theta$	?	-10	6



So (→):  $S = ut + \frac{1}{2} at^2$   
 $\therefore 240 = (u \cos \theta)(6) + 0$   
 $\Rightarrow u \cos \theta = 40$  (a)

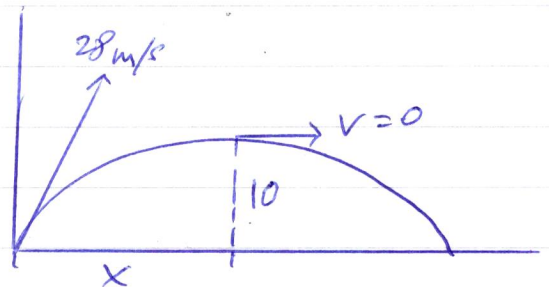
(↑):  $S = ut + \frac{1}{2} at^2 \Rightarrow 0 = (u \sin \theta)(6) - \frac{1}{2}(10)6^2$   
 $\Rightarrow u \sin \theta = 30$  (b)

use (a) & (b):  $u^2 \cos^2 \theta + u^2 \sin^2 \theta = 40^2 + 30^2$   
 So  $u^2 (\cos^2 \theta + \sin^2 \theta) = 1600 + 900 = 2500$   
 $\therefore u = 50 \text{ m/s}$

(since  $\cos^2 \theta + \sin^2 \theta = 1$ )

and  $\tan \theta = \frac{u \sin \theta}{u \cos \theta} = \frac{30}{40} \Rightarrow \theta = 36.87^\circ$  direction

(18)	S	U	V	A	T
(→)	x	$28 \cos \theta$	0	0	t
(↑)	10	$28 \sin \theta$	0	-9.8	t

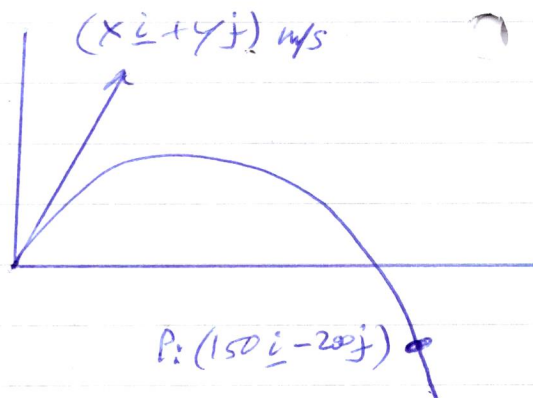


Note: At max ht  $v = 0$ .

So (↑):  $v^2 = u^2 + 2as \Rightarrow 0 = (28 \sin \theta)^2 - 2(9.8)(10)$

$\Rightarrow \sin \theta = \sqrt{\frac{196}{28^2}} = \frac{1}{2}, \therefore \theta = 30^\circ$

(19)	S	U	V	A	T
(→)	150	x		0	10
(↑)	-200	y		-9.8	10



$$\text{So } (\rightarrow) : S = ut + \frac{1}{2} at^2$$

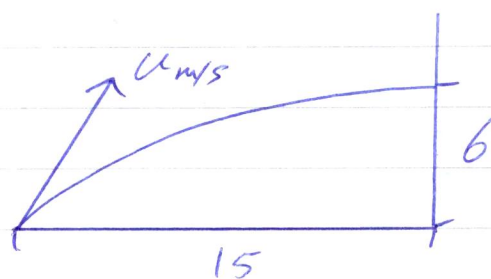
$$\therefore 150 = (x)(10) \Rightarrow x = 15$$

$$(\uparrow) : S = ut + \frac{1}{2} at^2 \Rightarrow -200 = (y)(10) - \frac{1}{2}(9.8)(100)$$

$$\therefore y = 29$$

$$\therefore \underline{u} = (15\hat{i} + 29\hat{j}) \text{ m/s}$$

(20)	S	U	V	A	T
(→)	15	x		0	3
(↑)	6	y		-10	3



$$\text{So } (\rightarrow) : S = ut + \frac{1}{2} at^2 \Rightarrow 15 = 3x \Rightarrow x = 5 \text{ m}$$

$$(\uparrow) : S = ut + \frac{1}{2} at^2 \Rightarrow 6 = 3y - \frac{1}{2}(10)(9)$$

$$\therefore y = 17 \text{ m}$$

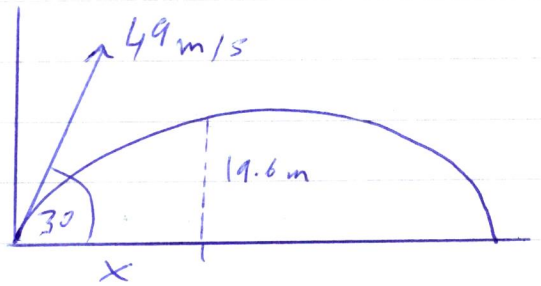
(21) Exactly same type of problem as (20), obtaining  $x = 11 \text{ m}$

$$\& y = 11 \text{ m} . \text{ Then } u = \sqrt{11^2 + 11^2} = 15.56 \text{ m/s}$$

$$\& \text{ direction : } \theta = \tan^{-1} \frac{11}{11} = 45^\circ .$$

(22)

	S	U	V	A	T
(→)	x	49 cos 30	0	0	t
(↑)	19.6	49 sin 30	-	-9.8	t



So (→):  $S = ut + \frac{1}{2} at^2 \Rightarrow x = (49 \cos 30)t + 0$

(↑):  $S = ut + \frac{1}{2} at^2 \Rightarrow 19.6 = (49 \sin 30)t - \frac{1}{2} (9.8)t^2$

$\Rightarrow 4.9t^2 - 24.5t + 19.6 = 0$

$\therefore t = 1, 4$  seconds

$\Rightarrow$  time for particle to remain at least at a height of 19.6 m is  $t = 4 - 1 = 3$  seconds

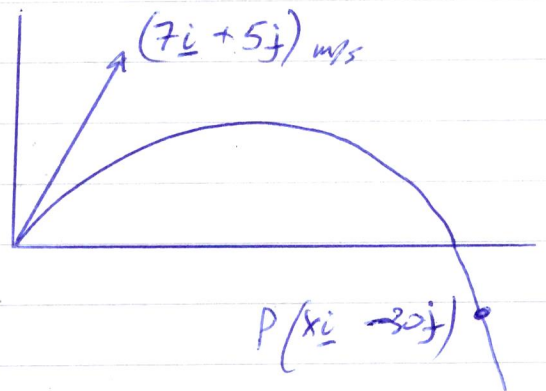
(Note: 19.6 m is Not max height)

(23) Same as (22). Quadratic is  $t^2 - 8t + 12 = 0$   
 $\Rightarrow t = 2, 6$  seconds

$\therefore$  time for particle to be at least 60 m high is  $t = 6 - 2 = 4$  sec

(24)

	S	U	V	A	T
(→)	x	7	0	0	t
(↑)	-30	5	-	-10	t



So (↑):  $S = ut + \frac{1}{2} at^2$

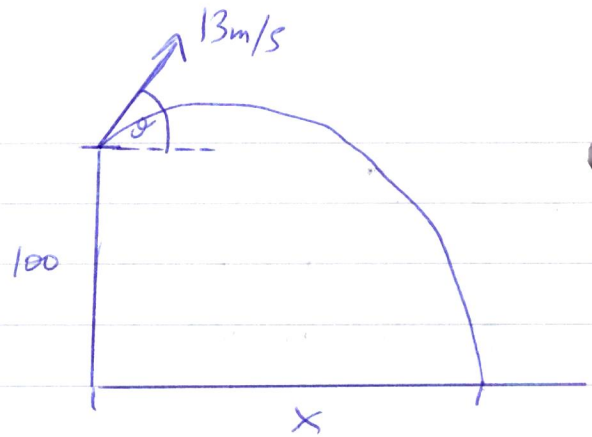
$\Rightarrow -30 = 5t - \frac{1}{2} (10)t^2$

$\Rightarrow t^2 - t - 6 = 0, \therefore (t - 3)(t + 2) = 0 \Rightarrow t = 3$  seconds

Now (→):  $S = ut + \frac{1}{2} at^2 \Rightarrow x = 7(3) = 21$  m

25

S	U	V	A	T	
(→)	x	13 cos θ	0	0	t
(↑)	-100	13 sin θ	-10	t	



Note:  $S = -100$  for (↑) because Stone has fallen by 100m

$$\tan \theta = \frac{5}{12}$$

$$\therefore (\uparrow): S = ut + \frac{1}{2} at^2$$

$$\Rightarrow -100 = \left[ 13 \cdot \left( \frac{5}{13} \right) \right] t - \frac{1}{2} (10) t^2$$

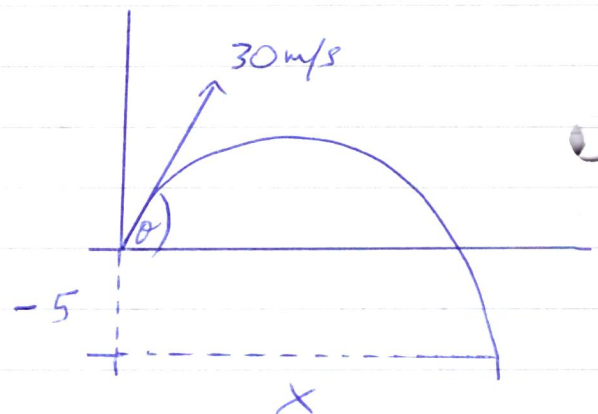
$$\Rightarrow t^2 - t - 20 = 0 \Rightarrow (t - 5)(t + 4) = 0$$

$$\therefore t = 5 \text{ sec}$$

$$\text{For } (\rightarrow): S = ut + \frac{1}{2} at^2 \Rightarrow x = \left[ 13 \left( \frac{12}{13} \right) \right] (5) = 60 \text{ m.}$$

26

S	U	V	A	T	
(→)	x	30 cos θ	0	0	t
(↑)	-5	30 sin θ	-10	t	



$$\text{So } (\uparrow): S = ut + \frac{1}{2} at^2$$

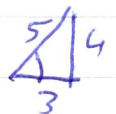
$$\Rightarrow -5 = 30 \left( \frac{4}{5} \right) t - \frac{1}{2} (10) t^2$$

$$\Rightarrow 5t^2 - 24t - 5 = 0$$

$$\Rightarrow (5t + 1)(t - 5) = 0$$

$$\therefore t = 5 \text{ seconds}$$

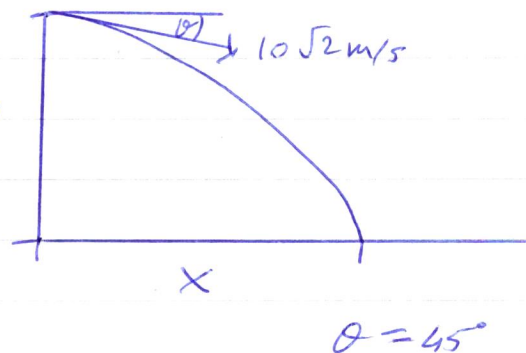
$$\tan \theta = \frac{4}{3}$$



$$\text{From } (\rightarrow): S = ut + \frac{1}{2} at^2 \Rightarrow x = 30 \left( \frac{3}{5} \right) (5) = 90 \text{ m.}$$

(27)

S	U	V	A	T
(→) x	$10\sqrt{2} \cos \theta$	0	0	t
(↑) y	$10\sqrt{2} \sin \theta$	-10	0	t



So (↑):  $S = ut + \frac{1}{2} at^2$

$$\therefore -40 = (10\sqrt{2} \sin 45^\circ)t - \frac{1}{2}(10)t^2$$

$$\therefore 5t^2 + (10\sqrt{2} \sin 45^\circ)t - 40 = 0$$

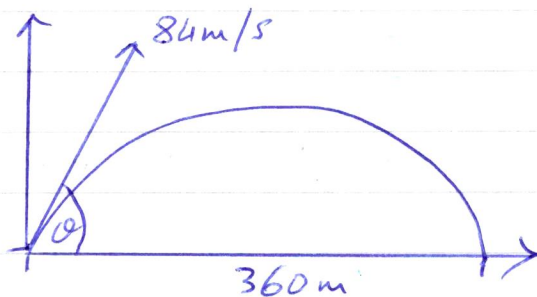
$$\Rightarrow t^2 + 2t - 8 = 0$$

$$\therefore (t+4)(t-2) = 0 \Rightarrow t = 2 \text{ sec.}$$

(→):  $S = ut + \frac{1}{2} at^2 \Rightarrow x = (10\sqrt{2} \cos 45^\circ) \cdot (2) = 20 \text{ m}$

(28)

S	U	V	A	T
(→) x	$84 \cos \theta$	0	0	t
(↑) y	$84 \sin \theta$	-9.8	0	t



So (→):  $S = ut + \frac{1}{2} at^2$

$$\therefore 360 = (84 \cos \theta)t + 0$$

$$\Rightarrow t = \frac{360}{84 \cos \theta} \quad (1)$$

(↑):  $S = ut + \frac{1}{2} at^2 \Rightarrow 0 = (84 \sin \theta)t - \frac{1}{2}(9.8)t^2$

By (1):  $0 = (84 \sin \theta) \left( \frac{360}{84 \cos \theta} \right) - 4.9 \left( \frac{360}{84 \cos \theta} \right)^2$

So  $0 = (\sin \theta \cdot \cos \theta) (360) - (4.9) \left( \frac{360}{84} \right)^2$

$$\Rightarrow \frac{360}{4.9} \sin \theta \cdot \cos \theta = \left( \frac{360}{84} \right)^2 \Rightarrow \frac{1}{2} \sin 2\theta = \left( \frac{360}{84} \right)^2 \left( \frac{4.9}{360} \right)$$

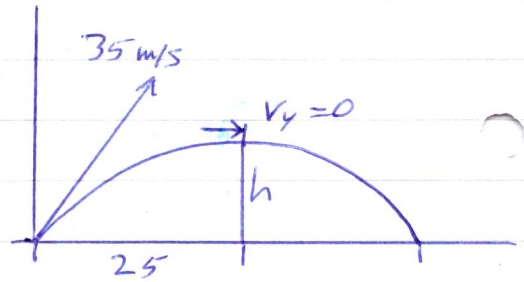
$$\textcircled{S} \quad \frac{1}{2} \sin 2\theta = \frac{1}{4} \Rightarrow \sin 2\theta = \frac{1}{2}$$

$$\therefore 2\theta = 30 \pm 360n \quad \& \quad 2\theta = 150 \pm 360n, \quad n = 1, 2, \dots$$

$$\therefore \theta = 15^\circ \text{ or } 75^\circ$$

(29) Same as (28)

(30)	S	U	V	A	T
(→)	25	$35 \cos \theta$		0	t
(↑)	h	$35 \sin \theta$	0	-9.8	t



$$\text{So } (\rightarrow): S = ut + \frac{1}{2} at^2 \Rightarrow 25 = (35 \cos \theta)t + 0$$

$$\therefore t = \frac{25}{35} \cdot \frac{1}{\cos \theta} \quad \textcircled{1}$$

$$(\uparrow): v = u + at \Rightarrow 0 = (35 \sin \theta) - 9.8t$$

$$\Rightarrow t = \frac{35}{9.8} \cdot \frac{1}{\sin \theta} \quad \textcircled{2}$$

$$\text{Then } \textcircled{1} = \textcircled{2}: \quad \frac{25}{35} \cdot \frac{1}{\cos \theta} = \frac{35}{9.8} \cdot \frac{1}{\sin \theta}$$

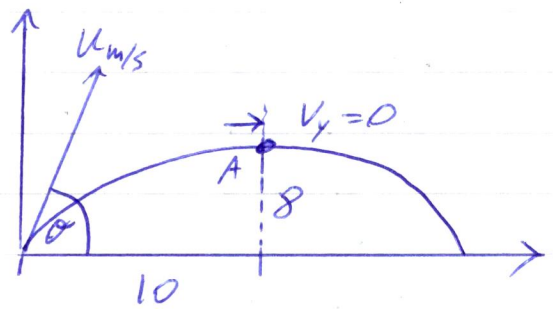
$$\text{So } \frac{(25)(9.8)}{35^2} = \sin \theta \cos \theta = \frac{1}{2} \sin 2\theta$$

$$\therefore \sin 2\theta = 0.4$$

$$\Rightarrow 2\theta = 23.58^\circ, 156.42^\circ$$

$$\therefore \theta = 11.79^\circ, 78.21^\circ$$

	S	U	V	A	T
(→)	10	$u \cos \theta$		0	t
(↑)	8	$u \sin \theta$		-9.8	t



$$\text{So } (\rightarrow): S = ut + \frac{1}{2}at^2 \Rightarrow 10 = (u \cdot \cos \theta) t$$

$$\therefore t = \frac{10}{u \cdot \cos \theta} \quad (1)$$

$$(\uparrow): v = u + at \Rightarrow 0 = (u \cdot \sin \theta) - 9.8 t$$

$$\therefore t = \frac{u \cdot \sin \theta}{9.8} \quad (2)$$

$$\underline{(1) = (2)}:$$

$$\frac{10}{u \cdot \cos \theta} = \frac{u \cdot \sin \theta}{9.8}$$

$$\Rightarrow \frac{98}{\cos \theta \cdot \sin \theta} = u^2 \quad (3)$$

$$\text{But Also } (\uparrow): v^2 = u^2 + 2as \Rightarrow 0 = (u \sin \theta)^2 - 2(9.8)(8)$$

$$\Rightarrow \frac{156.8}{\sin^2 \theta} = u^2 \quad (4)$$

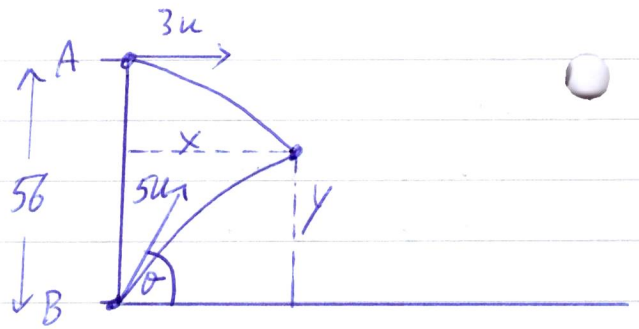
$$\underline{\text{So } (3) = (4)}: \frac{156.8}{\sin^2 \theta} = \frac{98}{\cos \theta \cdot \sin \theta}$$

$$\therefore \frac{156.8}{98} = \tan \theta \Rightarrow \theta = 58^\circ \text{ above horizontal}$$

$$\text{By } (4): \frac{156.8}{(\sin 58) ^2} = u^2 \Rightarrow u = 14.77 \text{ m/s}$$

32

	S	U	V	A	T
A: ( $\rightarrow$ )	X	3u	0	0	2
( $\uparrow$ )	56-y	0		-9.8	2
B: ( $\rightarrow$ )	X	5u \cos	0	0	2
( $\uparrow$ )	Y	5u \sin		-9.8	2



For B: ( $\uparrow$ ):  $S = ut + \frac{1}{2}at^2 \Rightarrow y = (5u \sin \theta)(2) - \frac{1}{2}(9.8)(4)$

$$\therefore \frac{y}{2} + 9.8 = 5u \sin \theta \quad (1)$$

( $\rightarrow$ ):  $S = ut + \frac{1}{2}at^2 \Rightarrow x = (5u \cos \theta)(2)$   
 $= 10u \cos \theta \quad (2)$

For A: ( $\uparrow$ ):  $56 - y = 0 - \frac{1}{2}(9.8)(4) \Rightarrow y = 36.4 \text{ m} \quad (3)$

( $\rightarrow$ ):  $x = (3u)(2) + 0 = 6u \quad (4)$

(2) into (4):  $6u = 10u(\cos \theta) \Rightarrow \theta = 53.13^\circ$

using y & theta in (1):  $\frac{36.4}{2} + 9.8 = 5u \cdot \sin 53.13$

$$\therefore u = 7 \text{ m/s}$$

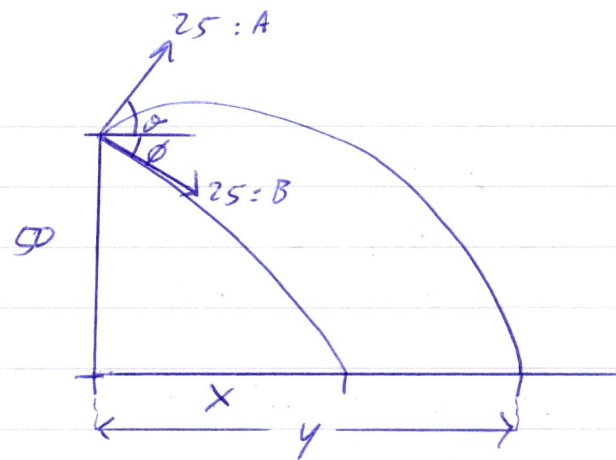
using u & theta in (2):  $x = 10(7) \cos 53.13 = 42 \text{ m}$

(33)

(A) S U V A T

$$\rightarrow y \quad 25 \cos \theta \quad 0 \quad 0 \quad t$$

$$\uparrow -50 \quad 25 \sin \theta \quad -10 \quad t$$



(B)

$$\rightarrow x \quad 25 \cos \theta \quad 0 \quad 0 \quad t$$

$$\uparrow -50 \quad 25 \sin \theta \quad -10 \quad t$$

$$\tan \theta = \frac{3}{4}; \tan \phi = \frac{3}{4}$$



For A:  $\uparrow$ :  $s = ut + \frac{1}{2} at^2$

$$\Rightarrow -50 = 25 \left(\frac{3}{5}\right)t - \frac{1}{2} \cdot 10t^2$$

$$\Rightarrow t^2 - 3t - 10 = 0 \Rightarrow (t-5)(t+2) = 0 \Rightarrow \underline{t=5}$$

$\therefore$  A takes 5 secs to land

For B:  $\uparrow$ :  $s = ut + \frac{1}{2} at^2 \Rightarrow -50 = (25 \sin \phi)t - \frac{1}{2} \cdot 10 \cdot t^2$

$$\sin \phi = -\frac{3}{5} \quad (\text{Not } \frac{3}{5}) \quad \therefore t^2 + 3t - 10 = 0$$

leading to  $(t+5)(t-2) = 0 \Rightarrow \underline{t=2}$ ; B takes 2 secs to land

$\therefore$  time interval between B & A is 3 secs

For y & x: A  $\uparrow$ :  $s = ut + \frac{1}{2} at^2 \Rightarrow y = (25 \cos \theta) \cdot t + 0$   
 $= 25 \left(\frac{4}{5}\right) \cdot 5 = 100 \text{ m}$

B  $\uparrow$ :  $s = ut + \frac{1}{2} at^2 \Rightarrow x = (25 \cos \phi) \cdot t + 0$   
 $= 25 \left(\frac{4}{5}\right) \cdot 2 = 40 \text{ m}$

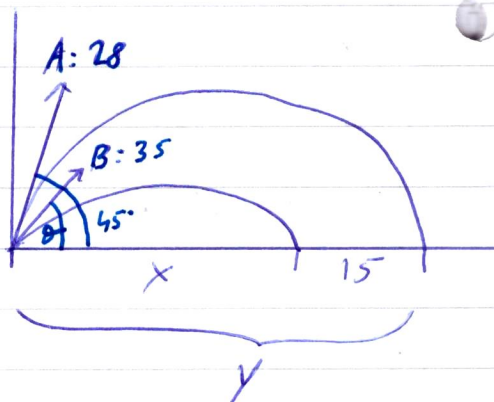
So distance between landings = 60 m.

(\*)

(34)

	S	U	V	A	T
<u>A:</u>	(→) y	$28 \cos \theta$	0	0	t
	(↑)	$28 \sin \theta$		-9.8	t

<u>B:</u>	(→) x	$35 \cos \theta$	0	0	t
	(↑)	$35 \sin \theta$		-9.8	t



So A: (→) :  $y = x + 15 = (28 \cos 45) t + 0$  (1)

(↑) :  $0 = (28 \sin 45) t - \frac{1}{2} (9.8) t^2$  (2)

(all by  $s = ut + \frac{1}{2} at^2$ ).

For B: (→) :  $s = ut + \frac{1}{2} at^2 \Rightarrow x = (35 \cos \theta) t + 0$  (3)

(↑) :  $s = ut + \frac{1}{2} at^2 \Rightarrow 0 = (35 \sin \theta) t - \frac{1}{2} (9.8) t^2$  (4)

By (2):  $4.9 t^2 - \frac{28}{\sqrt{2}} t = 0 \Rightarrow t (4.9 t - \frac{28}{\sqrt{2}})$

So  $t=0$  or  $4.9 t = \frac{28}{\sqrt{2}} \Rightarrow t = 4.04 \text{ sec}$  (5)

(5) into (1):  $x + 15 = (28 \cos 45) (4.04) \Rightarrow x = 80 - 15 = 65 \text{ m}$

Now use (3):  $65 = (35 \cos \theta) t \Rightarrow t = \frac{65}{35 \cos \theta}$

Now use (4):  $0 = \frac{(35 \sin \theta) \cdot 65}{35 \cos \theta} - 4.9 \left( \frac{65}{35 \cos \theta} \right)^2$  (6)

(6) simplifies to  $\sin \theta \cos \theta = \frac{(4.9)(65)}{35^2}$ , i.e.  $\frac{1}{2} \sin 2\theta = 0.26$

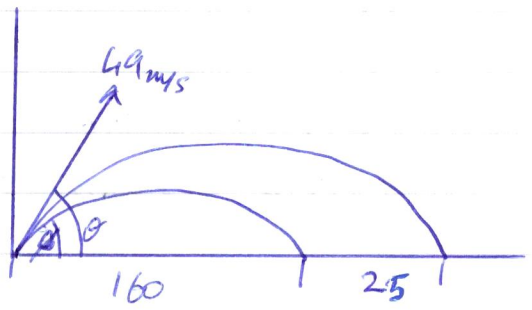
So  $\theta = 15.66^\circ$  &  $74.33^\circ$

35

	S	U	V	A	T
--	---	---	---	---	---

(→) 185    49 cos θ    0    0    t

(↑) 0    49 sin θ    -9.8    t



(→) 180    49 cos φ    0    0    t

(↑) 0    49 sin φ    -9.8    t

So (→) :  $S = ut + \frac{1}{2} at^2 \Rightarrow 185 = (49 \cos \theta)t + 0$  (1)

and  $180 = (49 \cos \phi)t + 0$  (2)

(↑) :  $S = ut + \frac{1}{2} at^2 \Rightarrow 0 = (49 \sin \theta)t - \frac{1}{2} \cdot 9.8t^2$  (3)

and  $0 = (49 \sin \phi)t - \frac{1}{2} \cdot 9.8t^2$  (4)

By (1):  $t = \frac{185}{49 \cos \theta}$

Into (3):  $0 = \frac{(49 \sin \theta) \cdot 185}{49 \cos \theta} - 4.9 \left( \frac{185}{49 \cos \theta} \right)^2$

$\Rightarrow 0 = 185 \frac{\sin \theta}{\cos \theta} - \frac{4.9 \cdot 185^2}{49^2 \cos^2 \theta}$

$\Rightarrow 185 \sin \theta \cos \theta = \frac{4.9 \cdot 185^2}{49^2}$

$\Rightarrow \frac{1}{2} \sin 2\theta = \frac{(4.9)(185)}{49^2} = 0.377$

So  $2\theta = 49.03^\circ \neq 130.96^\circ$

So  $\theta = 24.52^\circ \neq 65.48^\circ$

By the same process, using (2) into (4) we get

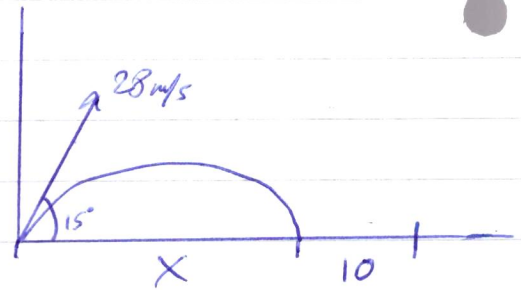
$\frac{1}{2} \sin 2\phi = 0.377$

leading to  $\phi = 20.387^\circ, 69.61^\circ$

So we can have  $20.39^\circ \rightarrow 24.52^\circ$  &  $65.48^\circ \rightarrow 69.61^\circ$

36

	S	U	V	A	T
(→)	X	28 cos 15	?	0	t
(↑)	0	28 sin 15	?	-9.8	t



So (→) :  $S = ut + \frac{1}{2}at^2 \Rightarrow X = (28 \cos 15)t + 0$  (1)

(↑) :  $S = ut + \frac{1}{2}at^2 \Rightarrow 0 = (28 \sin 15)t - \frac{1}{2}(9.8)t^2$  (2)

By (2) :  $t(4.9t - 28 \sin 15) = 0 \Rightarrow t = 1.479 \text{ sec}$  (3)

(3) into (1) gives  $X = (28 \cos 15)(1.479) = 60 \text{ m}$

So boundary is  $60 + 10 = 70 \text{ m}$  away.

Now we have

	S	U	V	A	T
(→)	50	$u \cos 15$		0	t
(↑)	0	$u \sin 15$		-9.8	t

So (↑) :  $S = ut + \frac{1}{2}at^2 \Rightarrow 0 = (u \sin 15)t - \frac{1}{2}(9.8)t^2$  (4)

(→) :  $S = ut + \frac{1}{2}at^2 \Rightarrow 50 = (u \cos 15)t$  (5)

By (5) :  $t = \frac{50}{u \cos 15}$ . This into (4) gives

$$0 = (u \sin 15) \left( \frac{50}{u \cos 15} \right) - 4.9 \left( \frac{50}{u \cos 15} \right)^2$$

$$\Rightarrow u^2 \cdot \cos 15 \cdot \sin 15 = (4.9)(50)$$

$$u^2 \cdot \frac{1}{2} \sin 30 = (4.9)(50)$$

$$\Rightarrow u^2 = 980, \therefore u = 31.3 \text{ m/s}$$